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# Effect of coarse aggregate size and cement paste volume on concrete behavior under high triaxial compression loading

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# ABSTRACT

When massive concrete structures (high-rise buildings, tunnels, dams, nuclear power plants, bridges, protection structures, ...) are subjected to extreme loadings (aircraft shocks, rock falls, near-field detonations, ballistic impacts, ...), the material undergoes triaxial compression loading at a high confinement. In order to reproduce high stress levels with well-controlled loading paths, static triaxial tests are carried out on concrete samples by mean of a very high-capacity triaxial press. It is a well-known fact that the cement paste volume and the coarse aggregate size are two important parameters of concrete formulation. This article focuses on identifying the effect of coarse aggregate size and cement paste volume on concrete behavior under high triaxial compression. This article shows that at low confinement, the concrete strength slightly increases as the coarse aggregate size increases. At high confinement, the coarse aggregate size has a slight influence on concrete deviatoric behavior and a significant influence on concrete strain limit-state. The higher the coarse aggregate size, the lower is the mean stress level corresponding to concrete strain limit-state. Furthermore, this article highlights that at low confinement, the concrete strength significantly increases with an increase in cement paste volume. Increasing confinement tends to reduce cement paste volume effect on concrete strength. At high confinement, contrary to what has been observed in unconfined compression, the cement paste volume has little effects on concrete deviatoric behavior. Otherwise, decreasing cement paste volume increases concrete deformation capacity. At very high confinement levels and at very high deviatoric stress levels, the axial tangent stiffness of concrete increases as the coarse aggregate size or the cement paste volume is reduced.

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# 1. Introduction

Concrete is employed in the building of highly sensitive infrastructure (high-rise buildings, tunnels, dams, nuclear power plants, bridges, protection structures, ...). Its mechanical behavior however is still rather poorly understood, especially under extreme dynamic loadings (impacts of vehicles or aircrafts, rock falls, near field detonation, ballistic impacts, ...). When subjected to violent dynamic loadings, concrete undergoes very high levels of triaxial stresses [1]. The validation of concrete constitutive models, taking into account simultaneously the brittle damage phenomena and irreversible strain in compaction, requires specific tests capable of reproducing complex loading paths.

The static characterization of a constitutive model to predict the dynamic behavior is not a new practice in the study of geomaterials. The rheological behavior of concrete under confined compression slightly depends on the strain rate for dried or wet specimens [2]. Thus, the strain rate effect in compression can be neglected in numerical simulations [3]. The strong loading rate dependency in tension can mainly be explained by the influence of propagation velocity of defects [4] and must be taken into account in simulations.

Most of the available experimental results in literature only relate to confined concrete behavior with moderate confining pressure [5–11]. These studies have particularly revealed the transition from brittle to ductile behavior that characterizes cohesive materials. Experimental studies on the triaxial behavior of cementitious materials under high confinement were carried out previously but they were limited to small mortar samples [12,13]. Some scarce triaxial test results on ordinary concrete with confining pressures ranging between 0 and 500 MPa are available in [1,14,15].

The results presented in this article make reference to static triaxial tests carried out on concrete samples by mean of a highcapacity hydraulic triaxial press, named the GIGA press. This experimental device makes it possible to reach, within concrete samples, stress levels on the order of one GPa with static, homogeneous and well-controlled load paths.

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Some previous results on the behavior under high confinement of the same reference ordinary concrete were obtained with the GIGA press. Gabet et al. studied the influence of loading path [16], Poinard et al. highlighted the damage process [17], Dupray et al. developed a mesoscopic model of these experiments [18], Vu et al. studied the influence of both the saturation ratio [19] and the water/cement ratio of concrete [20]. In particular, these results showed that under high confinement, the limit-state of the concrete remains relatively independent of both the loading path and Lode's angle, the saturation ratio exerts a major influence on concrete behavior and, when placed under high confinement, concrete behaves like a granular stacking composed of concrete without any influence from the level of cement matrix strength.

To the best of our knowledge, no results are available regarding the effects of coarse aggregate size and cement paste volume (or coarse aggregate volume) on concrete behavior when subjected to high triaxial compression loading, the present article focuses on these effects.

The experimental set-up used to perform the current study will be described in Section 2. Section 3 will present the main results concerning the effect of coarse aggregate size. Section 4 will introduce the influence of cement paste volume (or the influence of coarse aggregate volume). The presentation of the main conclusions and the outlook of the future work end the paper.

#### 2. Experimental set-up

The GIGA press is a large-capacity triaxial press, which has been specifically designed and developed for this study. Cylindrical concrete specimens ( $\emptyset = 70 \text{ mm}$ ; h = 140 mm) can be tested by applying confining pressures as large as 0.85 GPa and axial stresses up to 2.35 GPa. A picture of the press and a section of the specimen and of the loading apparatus are shown in Fig. 1 [34,35].

The concrete specimen, surrounded by a membrane impermeable to the confinement fluid, is placed between caps made of tungsten carbide. The instrumentation of the specimens consists of one Linear Variable Differential Transformers (LVDT) for measuring the axial displacement, one axial gauge and two circumferential gauges (Fig. 2).

The LVDT sensor used in this study is 500XS-3013 type from Schaevitz Sensors Company. The gauges (EP-08-10CBE-12 type from Vishay Micro-measurements Company) are 28 mm long. These gauges allow strain measurements up to 15%. Both the axial stress applied to the specimen and the pressure inside the cell are monitored by means of force and pressure sensors. The porous nature of the concrete requires the development of a protective multi-layer membrane surrounding the specimen in order to prevent the confining fluid from infiltrating the specimen [34,35] (see Fig. 2).

Compressive stresses and contraction strains are assumed to be positive; the following symbols are used:  $\sigma_x$  = principal axial stress; p = pressure inside the confining cell;  $\sigma_m$  = mean stress; q = principal-stress difference (deviatoric stress);  $\varepsilon_v$  = volumetric strain;  $\varepsilon_x$  = axial strain; and  $\varepsilon_\theta$  = circumferential strain:

$$\sigma_m = \frac{\sigma_x + 2p}{3}$$
  $q = \sigma_x - p$   $\varepsilon_v = \varepsilon_x + 2\varepsilon_\theta$ 

All tests were carried out according to the same triaxial compression loading procedure (Fig. 3). The test begins with a hydrostatic phase, during which confining pressure increases at a rate of 1.67 MPa/s until reaching the desired pressure. The confining pressure is applied on every surfaces of the sample through the membranes or through the two caps until the desired pressure p. Note that for all triaxial tests in this study, the sealing between the loading heads and the top and bottom ends of the concrete specimen is ensured by the multi-layer membrane placed around the specimen and supported over a part of the loading heads. Besides, for triaxial compression loading, there is no sealing between the loading heads and the piston (Fig. 1) [34]. The deviatoric phase is then conducted, at constant confining pressure, by imposing a constant displacement rate of  $20 \,\mu\text{m/s}$  for the axial jack. This rate corresponds to a strain rate of approximately  $10^{-4}$ /sec for the sample. Note that in all tests the maximum deviatoric stress value is not imposed, as a direct measure of the test. The unloading phase is symmetrical in comparison with the loading phase. Tests were carried out with the control of the confining pressure p and of the piston displacement (Fig. 1).

The unconfined compression tests were performed on a 100 tons Schenck press with a more adequate and accurate load sensor. These tests were controlled in displacement with a strain rate of approximately  $10^{-5}$ /sec. The concrete samples have the same dimensions as those used in the triaxial tests.

#### 3. Influence of coarse aggregate size

In order to study the effect of coarse aggregate size, from the mix design of the reference concrete (R30A7), two other concretes  $(d_{\min})$  and  $(D_{\max})$  were prepared with different maximum aggregate size  $(d_a)$ . Compared to concrete R30A7  $(d_a = 8 \text{ mm})$ , concrete  $d_{\min}$  has smaller aggregates  $(d_a = 3.15 \text{ mm})$ , while concrete  $D_{\max}$  has larger aggregates  $(d_a = 20 \text{ mm})$ .



Fig. 1. General view of the GIGA press (left) and cross-section of the confining cell (right).



Fig. 2. Instrumentation and protective membrane.



Fig. 3. Loading path of the completed tests: deviatoric stress q vs. confining pressure p;  $\sigma_x$ : axial stress;  $D_{max}$ ,  $d_{min}$ , R30A7,  $V_{pi}$ ,  $V_{ps}$ ; five concretes studied in this article.

# 3.1. Characteristics of concrete samples

# 3.1.1. Concrete composition

The modified mix designs are shown in Table 1, where the mix design of the reference concrete R30A7 is indicated as well. The

composition of the reference concrete, for which an exhaustive experimental study was carried out [16,17,19], is provided in the R30A7 column of Table 1. This reference concrete corresponds to an ordinary concrete in terms of both strength and slump. It displays a 28-days compressive strength of 30 MPa and a slump of

#### Table 1

Mix design and porosity of concretes  $d_{\min}$ ,  $D_{\max}$  and R30A7 characterized by different values of the maximum aggregate size  $(d_a)$ . " $D^{n(*)}$ : diameter of aggregates.

Concrete mix design $(kg/m^3)$ and porosity (%)	d <sub>min</sub>	R30A7	D <sub>max</sub>
2/3.15 mm "D" <sup>(*)</sup> gravel (d <sub>a</sub> = 3.15 mm)	1006		-
$0.5/20 \text{ mm "}D$ " gravel ( $d_a = 20 \text{ mm}$ )	-		995
$0.5/8 \text{ mm "}D" \text{ gravel } (d_a = 8 \text{ mm})$	-	1008	-
1800 μm "D" sand	838	838	838
CEM I 52.5N PM ES CP2 cement (Vicat)	263	263	263
Water	169	169	169
Porosity accessible to mercury (%)	11.5	12.6	10.7
Cement paste volume $(m^3/m^3 \text{ of concrete})$	0.29	0.29	0.29

7 cm. It can however be noted that the very high quality cement used, for purposes of better controlling material reproducibility, leads to a particularly low cement volume. Aggregates compound 99% quartzite are derived from natural deposit (rolled aggregates). Its maximal size (8 mm) was selected by taking the sample diameter (70 mm) into account.

Both modified mixes ( $d_{min}$  and  $D_{max}$ ) have the same cement paste volume (total volume of water, cement and occluded air measured in fresh concrete) and the same aggregate volume found in the reference mix (R30A7). Gravel 0.5/8 mm "D" is replaced with gravel 2/3.15 mm "D" in mix of  $d_{min}$  and with gravel 0.5/20 "D" in mix of  $D_{max}$ . Aggregates of concretes  $d_{min}$  and  $D_{max}$  also compound 99% quartzite are derived from natural deposit (rolled aggregates). The granulometric curves are given in Fig. 4. The porosity (Table 1) was measured by means of a high-pressure mercury-intrusion porosimeter. The values are similar because the three concretes have the same cement paste volume and the same aggregate volume.

The granulometry of concrete R30A7 was established by means of the rather empirical Dreux's method [36], in order to optimize the compactness of the granular skeleton. Hence, any change of coarse aggregate size with respect to the reference concrete leads to a non-optimal compactness of the granular skeleton. In more detail, any reduction of the coarse aggregate size contributes to the reduction of the compactness of the mix and to the increase of the friction between the cement paste and the aggregate particles. Conversely, any increase of coarse aggregate size implies a larger granular range and leads to a better compactness.

#### 3.1.2. Sample making and conservation

A suitable procedure for manufacturing the specimens was established in order to minimize the variability of concrete mechanical properties [34,35]. After cutting the extremities of the specimens to the desired length and smoothing the end sec-



Fig. 4. Granulometric curves of concretes R30A7 (reference),  $d_{\min}$  and  $D_{\max}$ .

tions, all specimens were stored in water for 3 months, in accordance with an identical curing procedure. The specimens were then dried about 4 months in a drying oven at 50 °C and 8% RH. Mass stabilization, however, was reached after 1 month, when the daily variation – after the spell inside the oven – did not exceed 0.1%.

## 3.2. Results of the triaxial tests

The behaviors of the three concretes  $d_{\min}$ ,  $D_{\max}$  and R30A7 during the triaxial tests carried out at no confinement (0 MPa, unconfined compression), at 100 MPa and 650 MPa are presented and discussed in the following. For each concrete, because of the identical procedures for conservation and making of all the tested samples, the mechanical properties of the different samples are thus quasi-equivalent to those of the samples tested in simple compression (Table 2).

### 3.2.1. Unconfined compression tests

In Figs. 5 and 6, the responses of the three concretes (R30A7,  $d_{\min}$ ,  $D_{\max}$ ) tested in unconfined compression are shown, in terms of mean stress vs. volumetric strain, and axial stress vs. circumferential and axial strains. The numerical values of Young's modulus E, ultimate stress  $\sigma_{\rm max}$  and Poisson's ratio v obtained for the three concretes (R30A7, d<sub>min</sub>, D<sub>max</sub>) are listed in Table 2. The slight differences of the volumetric behaviors (Fig. 5) are related to the small differences in terms of porosity (Table 1). Under unconfined compression, both the strength and the Young's modulus increase with the size of the coarse aggregate (Table 2 and Fig. 6). The strength and Young's modulus of concrete  $D_{max}$  are the largest and those of concrete  $d_{\min x}$  are the smallest. This phenomenon can be explained by the physical entanglement of aggregates that contributes to compressive strength and fracture energy of concrete and that is more pronounced with larger aggregates [25,26]. These results are coherent with those observed in the literature [21-26].

#### 3.2.2. Tests carried out at 100 MPa confinement

In Figs. 7 and 8, the results of the triaxial tests carried out on the three concretes ( $D_{max}$ , R30A7,  $d_{min}$ ) at 100 MPa confinement are shown. Fig. 7 shows that during the initial hydrostatic loading process, the volumetric responses of the three concretes are similar because of their similar porosities (see Table 1). Fig. 8 indicates that the conclusions obtained in the case of unconfined compression are still valid. At 100 MPa confinement level, concrete deviatoric behavior exhibits a stress threshold (peak deviatoric stress or extended plateau). This behavior can be explained by that at 100 MPa confinement, the cement matrix has not been sufficiently damaged during hydrostatic loading. At higher confinement level, when the cement matrix has completely damaged during hydrostatic loading the case shown in the next paragraph).

#### 3.2.3. Tests carried out at 650 MPa confinement

Figs. 9 and 10 (a close-up of Fig. 9) and 11 show the results of the triaxial tests carried out on the three concretes ( $D_{\text{max}}$ , R3A7,  $d_{\min}$ ) at 650 MPa confinement. Two tests were carried out on

#### Table 2

Unconfined compression tests carried out on the three concretes R30A7,  $d_{\min}$  and  $D_{\max}$ : identification of the main concrete characteristics.

Concrete	$d_{\min}$	R30A7	D <sub>max</sub>
Maximum aggregate size (mm)	3.15	8	20
Ultimate stress, $\sigma_{\max}$ (MPa)	41	42	48
Young's modulus, E (GPa)	21.6	24.0	26.7
Poisson's ratio, $v$	0.12	0.14	0.18



**Fig. 5.** Unconfined compression: plots of the mean stress  $\sigma_m$  vs. the volumetric strain  $\varepsilon_v$  for concretes R30A7 (*o*, solid line),  $d_{\min}$  (*x*, dash-dot line) and  $D_{\max}$  (triangle, dash line).



**Fig. 6.** Unconfined compression: plots of the axial stress  $\sigma_x$  vs. the strains  $\varepsilon_x$  and  $\varepsilon_\theta$  for concretes R30A7 (*o*, solid line),  $d_{\min}$  (*x*, dash-dot line) and  $D_{\max}$  (triangle, dash line).



**Fig. 7.** Triaxial compression at 100 MPa confinement: plots of the mean stress  $\sigma_m$  vs. the volumetric strain  $\varepsilon_v$  for concretes R30A7 (*o*, solid line),  $d_{\min}(x, \text{dash-dot line})$  and  $D_{\max}$  (triangle, dash line).

concrete  $d_{\min}$  ( $d_{\min-a}$  and  $d_{\min-b}$ ), but in the former test both the LVDT and the gauges were used, while in the latter test only the LVDT was active. These figures confirm previous findings.

The compaction processes of the three concretes in the hydrostatic phase of the loading are similar because of the similar porosities of the materials (Table 1). In the deviatoric phase, the largest volumetric strain is observed in concrete  $d_{\min}$ . Furthermore, there is a transition from contraction to dilatancy in concretes  $D_{\max}$ and R30A7. This transition can be identified in Fig. 10 (square symbol for concrete R30A7 and ellipse symbol for concrete  $D_{\max}$ ). In this figure, the contraction–dilatancy transition of concrete  $D_{\max}$  is ( $\sigma_m$ , q) = (906 MPa, 721 MPa) and that of concrete R30A7 is ( $\sigma_m$ , q) = (934 MPa, 830 MPa). This one corresponds to the



**Fig. 8.** Triaxial compression at 100 MPa confinement: plots of the stress deviator q vs. the strains  $\varepsilon_x$  and  $\varepsilon_\theta$  for concretes R30A7 (o, solid line),  $d_{\min}(x, \text{dash-dot line})$  and  $D_{\max}$  (triangle, dash line).



**Fig. 9.** Triaxial compression at 650 MPa confinement: plots of the mean stress  $\sigma_m$  vs. the volumetric strain  $\varepsilon_v$  for concretes R30A7 (*o*, solid line),  $d_{\min-a}$  (*x*, dash-dot line) and  $D_{\max}$  (triangle, dash line).



**Fig. 10.** Close-up of Fig. 9: triaxial compression at 650 MPa confinement: plots of the mean stress  $\sigma_m$  vs. the volumetric strain  $\varepsilon_v$  for concretes R30A7 (*o*, solid line),  $d_{\min-a}$  (*x*, dash-dot line) and  $D_{\max}$  (triangle, dash line). Contraction-dilatancy transition: square symbol for concrete R30A7 and ellipse symbol for concrete  $D_{\max}$ .

maximum volumetric-strain state, in terms of contraction in the material; and can be defined as the strain limit-state of the material. Dilatancy of the dried samples under high confinement is explained by a rearrangement of the granular stacking sequence composing the concrete. The shear stresses generate aggregate movement in the matrix, which initially serves to stimulate compaction. Once the maximum compaction level has been reached, the sample expands [16,17,19]. The mean stress level corresponding to this transition is slightly higher in concrete R30A7, whereas no contraction–dilatancy transition was observed in concrete  $d_{\min}$ , something that may be explained by observing that in this



**Fig. 11.** Triaxial compression at 650 MPa confinement: plots of the stress deviator q vs. the strains  $\varepsilon_x$  and  $\varepsilon_\theta$  for concrete samples R30A7 (o, solid line),  $d_{\min-a}(x, dash-dot line)$ ,  $d_{\min-b}$  (square, dash line) and  $D_{\max}$  (triangle, dash line).

concrete the maximum mean stress level (about 950 MPa) does not create the conditions for the contraction–dilatancy transition. Thus, the higher the size of coarse aggregate, the lower is the mean stress level corresponding to the concrete strain limit-state.

The three concretes have a hardening behavior (Fig. 11), as the confining pressure corresponding to the transition between brittle and hardening behaviors has been exceeded (the value of this confining pressure is close to 100 MPa for concrete R30A7 [20], see Fig. 8). Below this confining level, the cement matrix is still cohesive and it is mainly the cement matrix which contributes to concrete response [20]. Above this confining level, the cement matrix has lost its cohesion and it is the stacking of the aggregate particles which governs the concrete response (concrete behaves like a granular material). The ability of the aggregate particles to rotate under shear loading seems to be related to aggregate size. Thus, the higher the aggregate size, the lower is the deformation ability of the concrete.

Contrary to what has been observed in unconfined compression, at 650 MPa confinement, the differences between the plots of the deviatoric stress are rather limited (the maximum difference is about 160 MPa at 6% deviatoric strain). A more thorough examination of the curves in Fig. 11 shows that at high deviatoric strain levels (above 6%) the axial tangent stiffness of concrete  $d_{min}$  is higher than that of concrete  $D_{max}$ .

#### 4. Influence of the cement paste volume

The influence of the cement paste volume (or of the aggregate volume) with constant water/cement ratio, constant gravel/sand ratio and the same aggregate types is now presented.

## 4.1. Characteristics of concrete samples

Based on the composition of the reference concrete R30A7, two modified mix designs were adopted (Table 3). In comparison with the composition of the concrete R30A7, the first ( $V_{pi}$ ) has a cement paste volume (total volume of water, cement, occluded air measured in fresh concrete and possibly water-reducing additive) reduced by 0.04 m<sup>3</sup> (per 1 m<sup>3</sup> of concrete) and the second ( $V_{ps}$ ) has a cement paste volume increased by 0.04 m<sup>3</sup> (Table 3). A volume reduction of the cement paste with constant water/cement ratio requires the amount of water to be reduced; hence, it is necessary to add a water-reducing additive (Sikafluid) to guarantee a slump of at least 70 mm in concrete  $V_{pi}$ . Conversely, the concrete  $V_{ps}$  is more liquid and should not be vibrated, in order to avoid aggregate segregation. Casting, curing, machining and drying of the specimens made of concretes  $V_{pi}$  and  $V_{ps}$  were the same as for concrete

#### Table 3

Mix design and porosity of the three concretes tested to study the effect of cement paste volume. (\*)"D": diameter of aggregates.

Concrete mix design $(kg/m^3)$ and porosity (%)	$V_{\rm pi}$	R30A7	$V_{\rm ps}$
0.5/8 mm "D"(*) gravel	1064	1008	950
1800 μm "D" sand	885	838	791
CEM I 52.5N PM ES CP2 cement (Vicat)	221	263	304
Water (water reducing admixture Sikafluid)	138 (5.31)	169	196
Porosity accessible to mercury (%)	15.2	12.6	11.7
Cement paste volume $(m^3/m^3 \text{ of concrete})$	0.25	0.29	0.33

R30A7 (see Section 3.1.2). The values of the porosity accessible to mercury are presented in Table 3, where it is shown that the smaller the cement paste volume (or the larger the aggregate volume), the larger the porosity.

# 4.2. Results of the triaxial tests

The behavior of the three concretes  $V_{\rm pi}$ ,  $V_{\rm ps}$  and R30A7 during the triaxial tests carried out at no confinement (0 MPa, unconfined compression) and at 100 MPa and 650 MPa confinement is presented in the following. For each concrete, because of the identical procedures for conservation and making of all the tested samples, the mechanical properties of the different samples are thus quasiequivalent to those of the samples tested in simple compression (Table 4).

# 4.2.1. Unconfined compression tests

In Figs. 12 and 13, the responses of the three concretes ( $V_{pi}$ , R30A7,  $V_{\rm ps}$ ) tested in unconfined compression are shown, in terms of mean stress vs. volumetric strain and axial stress vs. circumferential and axial strains. The numerical values of Young's modulus *E*, ultimate stress  $\sigma_{\max}$  and Poisson's ratio v obtained for the three concretes ( $V_{\rm pi}$ , R30A7,  $V_{\rm ps}$ ) are listed in Table 4. Figs. 12 and 13 show that the volumetric strain decreases slightly, while the strength and the Young's modulus increase significantly following the increase of cement paste volume. The strength of concrete  $V_{ps}$ is 2.5 times higher than that of concrete  $V_{pi}$  (Fig. 13 and Table 4). In fact, the cohesive force between aggregates surfaces within the concretes  $V_{ps}$ , R30A7 and  $V_{pi}$  in hardened state depends on the cement paste volume filled in the voids between aggregates. With the same quality of cement paste (constant water/cement ratio), the constant gravel/sand ratio and the same aggregate types, the strength and the Young's modulus differences of the three studied concretes are mainly due to the cohesive force differences between aggregates surfaces of these concretes. Note that in comparison with the composition of the concrete R30A7, the concrete  $V_{pi}$  has a cement paste volume reduced by 0.04 m<sup>3</sup> (per 1 m<sup>3</sup> of concrete) and the concrete  $V_{ps}$  has a cement paste volume increased by 0.04 m<sup>3</sup> (Table 3). For the concrete  $V_{pi}$ , there is a lack of cement paste to fill all the voids between aggregates. Conversely, for the concrete  $V_{ps}$ , there is an excess of cement paste to fill all the voids between aggregates. Therefore, the cohesive force between aggregates surfaces within the concrete  $V_{pi}$  is the worst and the one within the concrete  $V_{ps}$  is the best. This

Table
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Unconfined compression tests carried out on the three concretes  $V_{pi}$ , R30A7,  $V_{ps}$ : identification of the main concrete characteristics.

Concrete	$V_{\rm pi}$	R30A7	$V_{\rm ps}$
Cement paste volume (m <sup>3</sup> /m <sup>3</sup> of concrete)	0.25	0.29	0.33
Ultimate stress, $\sigma_{\max}$ (MPa)	21	42	51
Young's modulus, E (GPa)	15.1	24.0	28.5
Poisson's ratio, $v$	0.12	0.14	0.16



**Fig. 12.** Unconfined compression: plots of the mean stress  $\sigma_m$  vs. the volumetric strain  $\varepsilon_v$  for concretes R30A7 (*o*, solid line),  $V_{\rm pi}$  (\*, dash-dot line) and  $V_{\rm ps}$  (diamond, dash line).



**Fig. 13.** Unconfined compression: plots of the axial stress  $\sigma_x$  vs. the strains  $\varepsilon_x$  and  $\varepsilon_\theta$  for concretes R30A7 (*o*, solid line),  $V_{\text{pi}}$  (\*, dash-dot line) and  $V_{\text{ps}}$  (diamond, dash line).



**Fig. 14.** Triaxial compression at 100 MPa confinement: plots of the mean stress  $\sigma_m$  vs. the volumetric strain  $\varepsilon_v$  for concretes R30A7 (*o*, solid line),  $V_{pi}$  (\*, dash-dot line) and  $V_{ps}$  (diamond, dash line).

explains the fact that the strength and the Young's modulus of concrete increase significantly as the cement paste volume increases (Table 4). Furthermore, as could be expected, an increase in the Poisson's ratio of the concrete can be observed with a increase of the cement paste volume (Table 4) because the concrete  $V_{\rm pi}$  is the most porous and the concrete  $V_{\rm ps}$  is the less porous (Table 3). These results are in agreement with the information available in the literature [27–33].

## 4.2.2. Tests carried out at 100 MPa confinement

Fig. 14 shows volumetric responses of the three concretes. In this figure, during the initial hydrostatic loading process, the volumetric strain of concrete  $V_{pi}$  is highest and that of concrete  $V_{ps}$  is lowest. This result is coherent with porosity differences of these concretes (Table 3).



**Fig. 15.** Triaxial compression at 100 MPa confinement: plots of the stress deviator q vs. the strains  $\varepsilon_x$  and  $\varepsilon_\theta$  for concretes R30A7 (o, solid line),  $V_{\rm pi}$  (\*, dash-dot line) and  $V_{\rm ps}$  (diamond, dash line).



**Fig. 16.** Triaxial compression at 650 MPa confinement: plots of the mean stress  $\sigma_m$  vs. the volumetric strain  $\varepsilon_v$  for concretes R30A7 (*o*, solid line),  $V_{pi}$  (\*, dash-dot line) and  $V_{ps}$  (diamond, dash line).



**Fig. 17.** Triaxial compression at 650 MPa confinement: plots of the stress deviator q vs. the strains  $\varepsilon_x$  and  $\varepsilon_\theta$  for concretes R30A7 (o, solid line),  $V_{\rm pi}$  (\*, dash-dot line) and  $V_{\rm ps}$  (diamond, dash line).

Fig. 15 presents deviatoric responses of the three concretes. One can observe a decrease, compared to the simple compression, of the difference between strengths of the three concretes. Furthermore, concrete  $V_{\rm ps}$  has a stress peak, followed by strain softening. Concrete R30A7 shows a ductile behavior with a horizontal plateau. Concrete  $V_{\rm pi}$  indicates a strain-hardening behavior.

## 4.2.3. Tests carried out at 650 MPa confinement

Figs. 16 and 17 show the results of the triaxial tests carried out on the three concretes ( $V_{ps}$ , R3A7,  $V_{pi}$ ) at 650 MPa confinement. At

very high confinement levels, a decrease of cement paste volume increases the deformation capacity (Fig. 16), because the phenomena observed at low confinement levels are reversed, as the cementitious matrix is no more cohesive. Fig. 17 indicates that at 650 MPa confinement, the differences between the deviatoric stress of the three concretes are rather limited (the maximum difference is about 200 MPa at 4% axial deviatoric strain). A more thorough observation of the curves in Fig. 17 highlights that for high deviatoric strain levels (above 6%), the larger the cement paste volume, the smaller the axial tangent stiffness of the concrete. Thus, at high confinement levels, any reduction of the cement paste volume increases the deformation capacity of the material; as a result, the deviatoric strain levels, the larger the cement paste volume. At high deviatoric strain levels, the larger the cement paste volume, the smaller the axial tangent stiffness.

#### 5. Conclusion and future work

This experimental investigation concerned the effect of coarse aggregate size and cement paste volume on concrete behavior under high triaxial compression loading. To identify this effect, a reference concrete was modified by varying only very few parameters. Triaxial tests were carried out on concrete samples for different coarse aggregate sizes (varying from 3 mm to 20 mm) or for different cement paste volumes (varying from 0.25 m<sup>3</sup> to 0.33 m<sup>3</sup>/1m<sup>3</sup> of concrete) and for confining pressure levels between 0 MPa and 650 MPa.

The coarse aggregate size has a slight influence on concrete deviatoric behavior as confinement levels vary from 0 MPa to 650 MPa. The concrete strength slightly increases as the coarse aggregate size increases as observed under unconfined compression. The coarse aggregate size has a significant influence on concrete strain limit-state at high confinement, the higher the coarse aggregate size, the lower is the mean stress level corresponding to concrete strain limit-state. At very high confinement levels and at very high deviatoric stress levels, the concrete axial tangent stiffness increases as the coarse aggregate size is reduced.

The cement paste volume has a significant effect on concrete behavior at low confinement. The concrete strength significantly increases with an increase in cement paste volume. Increasing confinement levels tends to reduce cement paste volume effect on concrete strength. At high confinement levels, contrary to what has been observed in unconfined compression, the cement paste volume has little effects on concrete deviatoric behavior. Otherwise, decreasing cement paste volume increases concrete deformation capacity. At very high confinement levels and at very high deviatoric stress levels, decreasing cement paste volume increases concrete axial tangent stiffness.

From an application standpoint, the presented results show that the strength of concrete, when subjected to extreme dynamic loading, is slightly influenced by the coarse aggregate size or by the cement paste volume for mean stress levels below 950 MPa and deviatoric stress levels below 900 MPa. This observation is contrary to the one issued from compression tests performed under moderate confinement, including unconfined compressive tests, in which the concrete compressive strength essentially depends on the cement paste quality and quantity and slightly depends on the coarse aggregate size. In reality, the cement is usually one of the most expensive constituents of concrete. The results shown in this article highlight the mechanical and economic advantages derived by reducing the cement paste volume (or the cement content) of concrete structures subjected to extreme loadings. Otherwise, many of the available protective design guidelines recommend the use of empirical approaches for the assessment of penetration, scabbing and perforation of concrete structures submitted to impacts [37]. All these empirical approaches consider the unconfined compressive strength as the only material parameter governing the resistance of concrete structures. The results presented in this article show the need to complement these empirical approaches to better take into account the influence of the granular skeleton of concrete into its resistance to impact.

As for the test set-up used in this study, axial stresses as large as 1.6 GPa can be applied to concrete specimens (diameter 70 mm; length 140 mm). However, the set-up will be partly modified in order to accommodate smaller specimens (diameter 50 mm; length 105 mm) in order to induce higher deviatoric stresses. In this way, the roles played by coarse aggregate size and cement paste volume will be more thoroughly investigated with reference to concrete deviatoric behavior.

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