

Fluid injection
into deformable geological formations
- energy related issues -

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Attaché ? dit le Loup : vous ne courez donc pas
Où vous voulez ? Pas toujours, mais qu'importe ?
Il importe si bien, que de tous vos repas
Je ne veux en aucune sorte,
Et ne voudrais pas même à ce prix un trésor.
Cela dit, maître Loup s'enfuit, et court encor.
Jean de La Fontaine, Fables, Livre 1, 1668

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